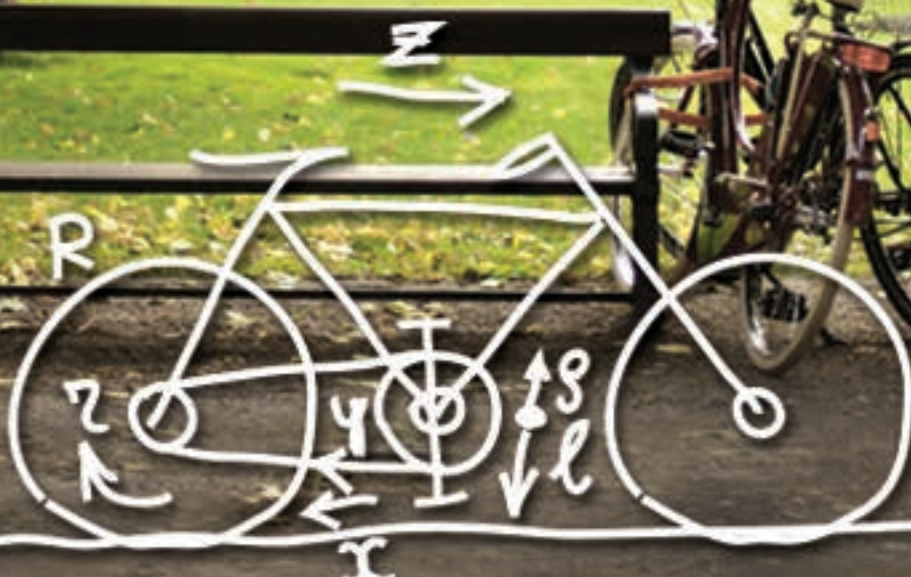


Mathematical Understanding of Nature

Essays on Amazing Physical Phenomena and
their Understanding by Mathematicians

V. I. Arnold



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